

## Assignment 1

1.

- **Availability:** Information can be reached at all times with the right keys. Eg. information queried is always available (no DDOS attacks preventing queries from reaching the server).
- **Integrity:** Assurance that information hasn't been modified, or if it has, an audit is kept with what is changed.
- **Confidentiality:** Protect information access, only being exposed to users who should have access.

1b) Most important: **confidentiality** given that a data breach would expose the health information of many patients (which may result in a data breach lawsuit).

1c) Both **integrity** and **availability** are equally important. Generally one would think about being able to access the alert system at all times, showing the importance of **availability**, however, to prevent others from sending unauthorized messages on the emergency system (such as turning on the tornado sirens when they shouldn't be) it would be more important to focus on **integrity**. (all sources from Lecture 1&2 slides)

2. In explaining Distributed Denial-of-Service (DDoS) attacks, it's important to understand Denial of Service (DoS) attacks. DoS attack is some attempt at "flooding" a host server from one IP/machine to overload the host server rendering the machine or network resource unavailable to the intended users. In a DDoS attack, there is more than one machine/user (usually from a botnet) that floods the host server, having a distributed load (instead of a single machine) attacking a server. DoS attacks were mostly used before firewalls were implemented, then after servers gained protection DDoS attacks were invented to go around these measures. Cite:

<https://security.stackexchange.com/a/22816/282055> and lecture 1 slide.

3. Yes, it's easily possible to break the Vigenère cypher (assuming the language is in English) in fact, one can break this cypher by hand (granted it would take a very long time but is possible). If the cypher has a lot of A's in it, one could assume they are E's in normal text (since E is the most common letter). Then, because there are a total possible  $26^n$  keys, where  $n = \text{key length}$ , it's easy to extrapolate the final plain text. Basically, once one knows the key length, they may treat the cypher as a Caesar cypher instead and solve from there. The process would look something like the following: Finding the key length (with Kasiski Examination), dividing the cypher, then

going through with Frequency Analysis on each group and decrypting the cypher from there. Cite: <https://crypto.stackexchange.com/a/73064> and Lecture 3 slides

- In principle (and definition), a perfectly secure system cannot be cracked as it is designed to be "perfect" against any attacks. That means even with a theoretical infinite computational power, it would still not be possible to crack the cypher. Of course, in practice, there is no such thing as a system that cannot be cracked given that there are always multiple points of failure (such as a key being lost, stolen, or reused). As from the Lecture 4 slides:

– A perfectly secure system

- does **NOT** mean there is no chance to get the plaintext!
- makes sure that **no attack strategy is better than a random guess!**

- Proof: (Citation from Lecture 4 Slides and <https://crypto.stackexchange.com/a/20749>)

$$Pr[C = c] = \sum Pr[C = c | M = m'] \cdot Pr[M = m'] = \sum Pr[K = m' \oplus c] \cdot Pr[M = m'] = \sum 2^{-n}$$

- (from bayes theorem)

$$Pr[M = m | C = c] = \frac{Pr[C = c | M = m] \cdot Pr[M = m]}{Pr[C = c]} = \frac{Pr[k = m \oplus c] \cdot Pr[M = m]}{2^{-n}} = \frac{2^{-n} \cdot 2^{-n}}{2^{-n}}$$

- No, Alice's design can still be broken. In replacing the One Time Pad method with a bit-wise AND & instead, we would obtain something like the following:

$$Pr[C = c] = \sum_M Pr[C = c | M = m] \cdot Pr[M = m] = \sum_{Pr[K=m' \wedge c]} \cdot Pr[M = m'] = \sum 2^{-n} \cdot Pr[M = m]$$

$$Pr[M = m | C = c] = \frac{Pr[C = c | M = m] \cdot Pr[M = m]}{Pr[C = c]} = \frac{Pr[K = m \wedge c] \cdot Pr[M = m]}{2^{-n}} = \frac{2^{-n} \cdot 2^{-n}}{2^{-n}}$$

This is quite an intuitive problem if one were to think about it. Basically, if a cypher character is 0 and the key is 0, then the plaintext would result in a 0 or 1 (with a 50/50 chance). Say we took the example input string of: 001101. Then taking  $M \wedge K$ :  $00110 \wedge 101110 = 001100$  revealing the first 2 bits and thus compromising the cipher. This could be explained with a probability formula like so:

$$\begin{aligned} P(C=1 | M=0) &= P(K \text{ AND } M = 1 | M=0) \\ &= P(K \text{ AND } 0 = 1 | M=0) \\ &= P(0=1 | M=0) \\ &= 0 \neq 2^{-1} \end{aligned}$$

- Source: <https://crypto.stackexchange.com/a/100827>

7. No, key reuse in a One Time Pad will result in a loss of perfect security and can be broken. As a reference to using a "many time pad attack", the steps to attack would be something like the following:

- 1) Guess one word appearing in the message
- 2) encode word from (1) to hex string
- 3) XOR both cypher texts
- 4) XOR hex string from (2) at each XOR position of both cyphers from (3)
- 5) When (4) is readable, guess the English word and expand the crib search.  
If not readable, try XOR of crib word at the next position

- Source for attack steps: <https://travisdazell.blogspot.com/2012/11/many-time-pad-attack-crib-drag.html>

The proof in pointing to the original proof from problem 5, we would have the two cyphers,  $C_1C_2$ , where would be some variation of  $C_i = M_i \oplus K$ , then knowing  $i$  cyphers (where  $i > 1$ ), they could compute the XOR of both ciphertexts like so:  $M_1 \oplus M_2 = C_1 \oplus C_2$ , hence if the attackers knows the structure of the plain text (assuming it's English), then can be able to observe patterns in both keys and result in a few of the values being compromised. This problem is quite similar to no.6 in the sense that perfect security is lost from giving the end user a few key parts of unencrypted data in order to figure out the last bit of data. Thus the reuse of one-time pad keys will result in an insecure system.

$$Pr[C = c] = \sum Pr[C = c|M = m'] \cdot Pr[M = m'] = \sum Pr[K = m' \oplus c] \cdot Pr[M = m'] = \sum 2^{-n} \cdot P$$

More formally, this could be displayed as:  $C_1 = M_1 \oplus K$   $C_2 = M_2 \oplus K$ , then  $C_1 \oplus C_2 = M_1 \oplus M_2$ , hence revealing the relationship between both plaintexts.